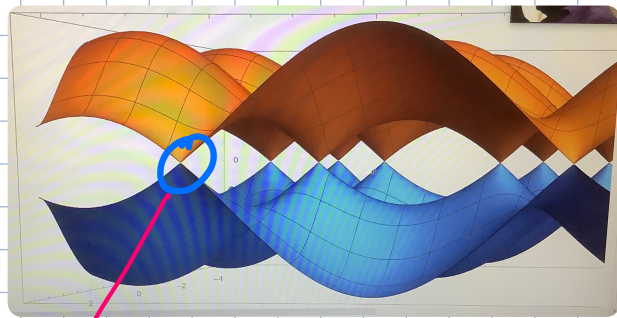
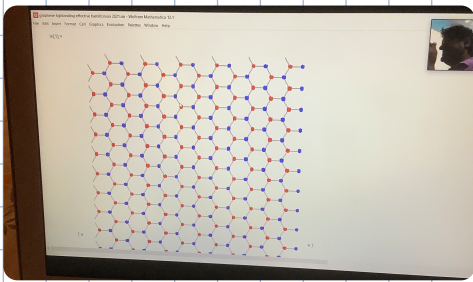


Review of tBM from previous class

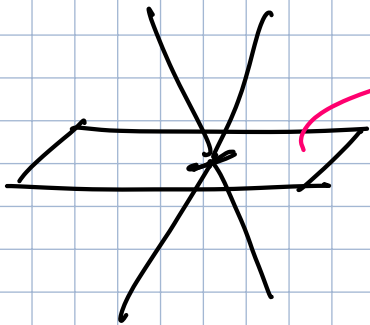
→ ssH
→ Graphene
→ CuD

Effective Hamiltonian of Graphene near touching points.



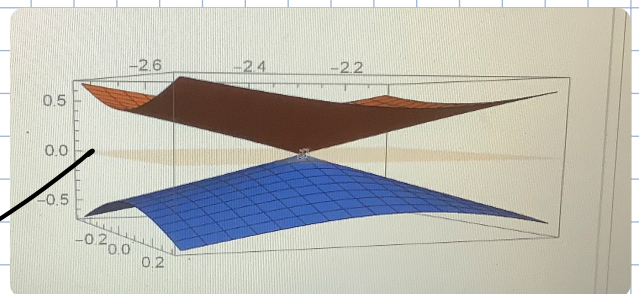
(Semi-metal)
→ low densities
→ complex but only at precise points
⇒ metals have more k-space areas where it's gapless.

→ p-orbitals → unhyb $1e^-$
↓
 $\frac{1}{2}$ filled
→ states arise from hybridisation of these orbitals



→ due to $1e^-$ of p-orbitals
⇒ $\frac{1}{2}$ filling

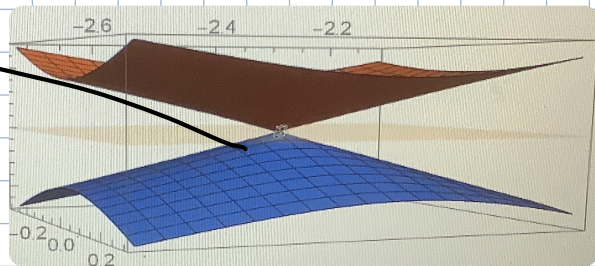
pristine graphene's Fermi energy



Taylor series expansion can be done in mathematica.

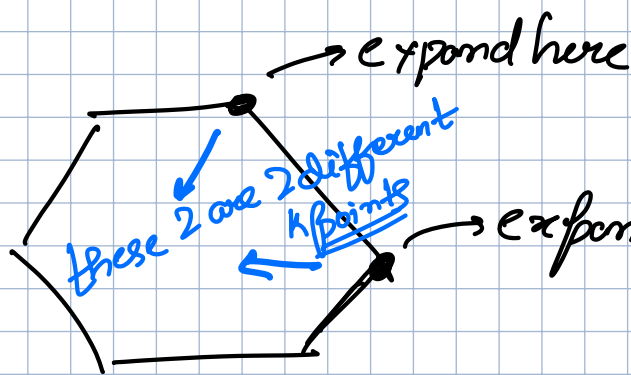
Effective Hamiltonian:-

- Linear dispersion for low energy excitations



$$H = \begin{pmatrix} 0 & \frac{-i(2+\sqrt{3})}{4} (q_x - i q_y) \\ \frac{i(2+\sqrt{3})}{4} (q_x + i q_y) & 0 \end{pmatrix}$$

$H = \vec{\sigma} \cdot \vec{p}$ → Dirac Hamiltonian for massless particles.



2 distinct k points

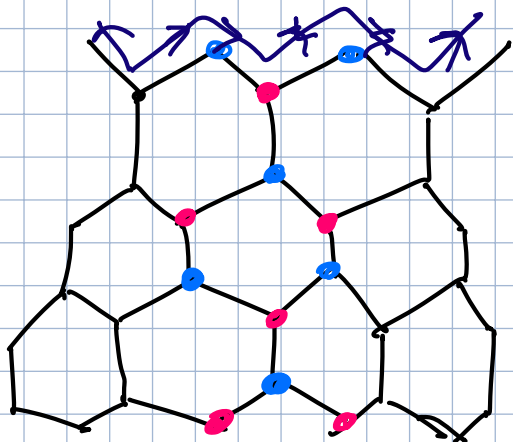
K K' (valleys)

Like A & B points in real space.

→ Structure of Hamiltonian is different at these K points.

Analogue of Gating for graphene

Let's consider a GNR.



Q. What are the electronic states present in GNR?

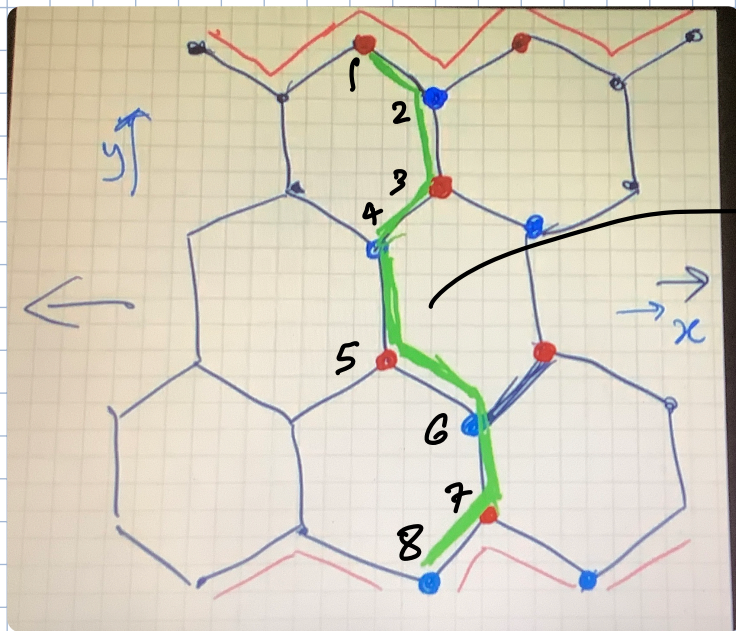
Motivatⁿ:- From ϕ Hc11, we know that edge states can be chiral & be ballistic.

We can see if something similar is

possible in Graphene.

How do we do it?

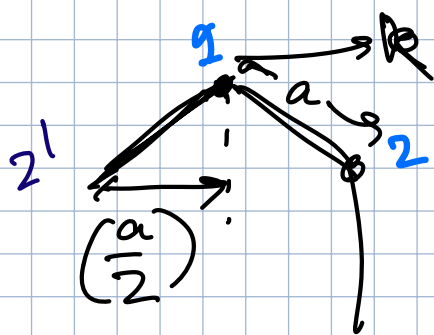
Brute force:- Define a Gigantic Unit cell.



Because y -directional translation symmetry is absent.

→ Call this a molecule

Now make a hopping matrix.

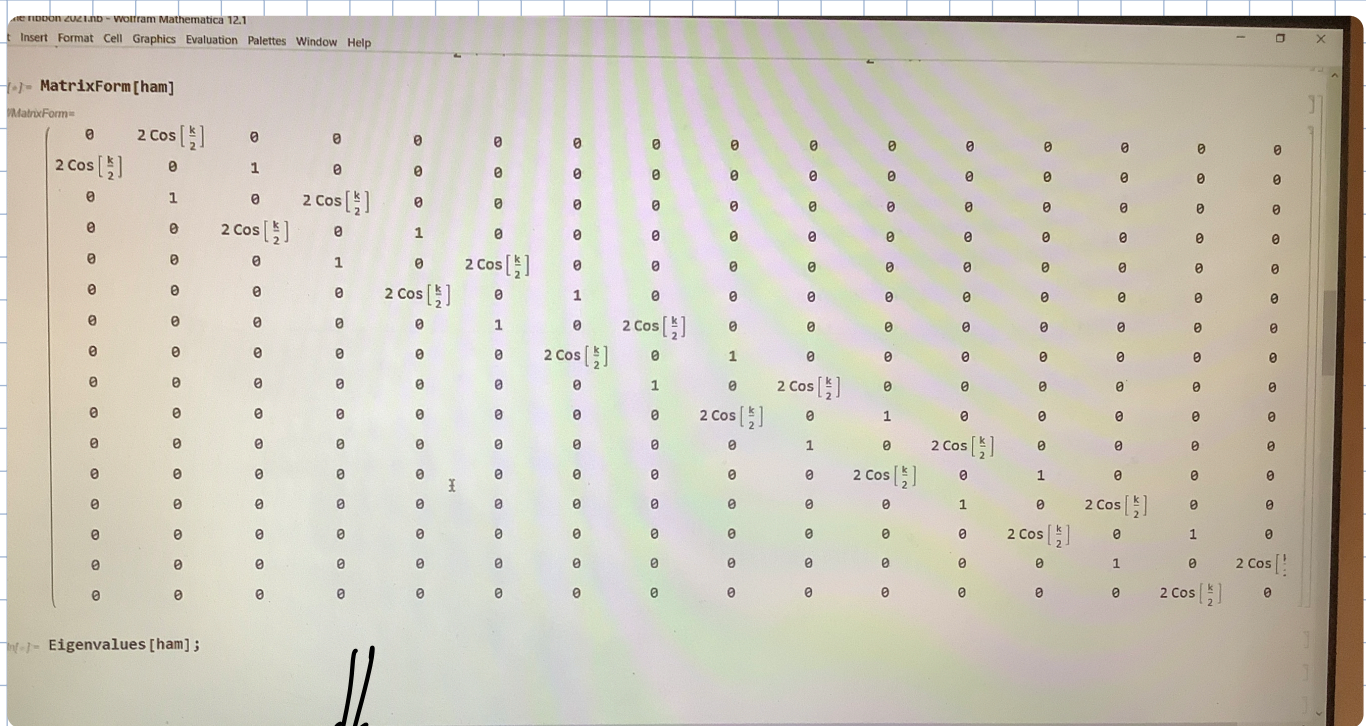


$$te^{-ikx_0} + te^{-ik\frac{a}{2}} \rightarrow \underline{\underline{Me}}$$

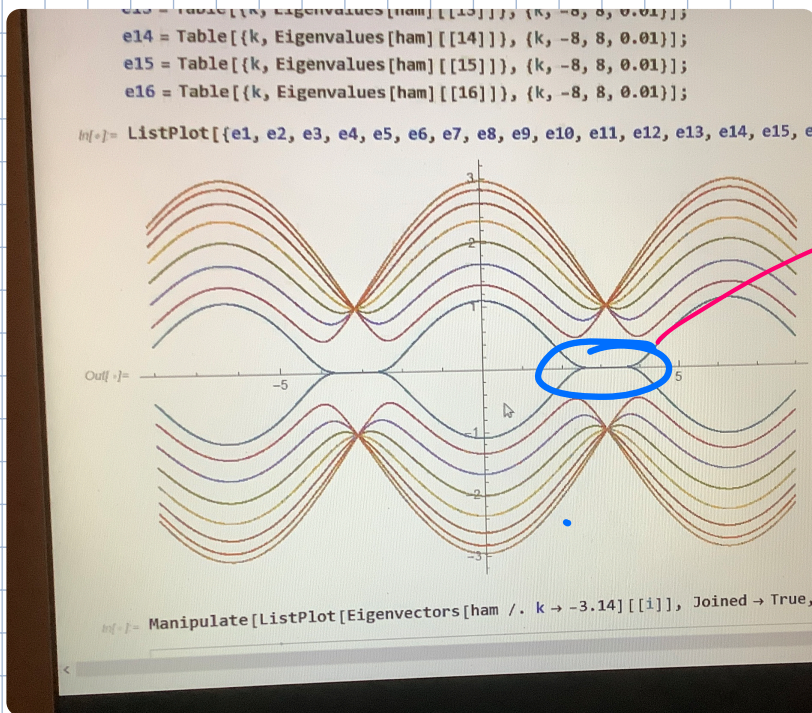
Disagreement:-

$$te^{-ik\frac{a}{2}} + te^{+ik\frac{a}{2}} \rightarrow \underline{\underline{MID}}$$

he's considering intracell non-trivial contributions as well



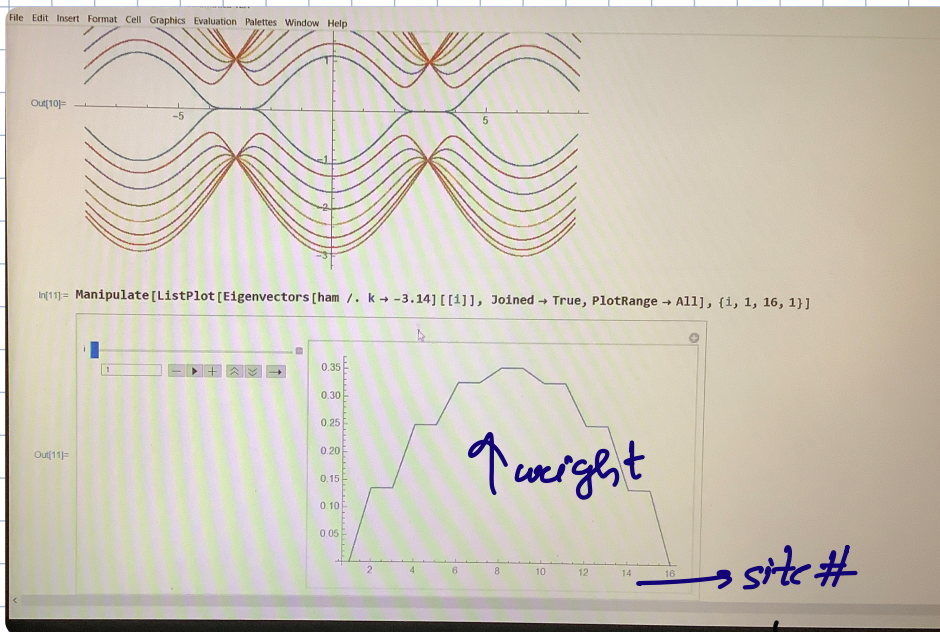
//
we'll get
16 bands



$k=\pi$, bands are flat
↓
looks like $v_g=0$, doesn't disperse.

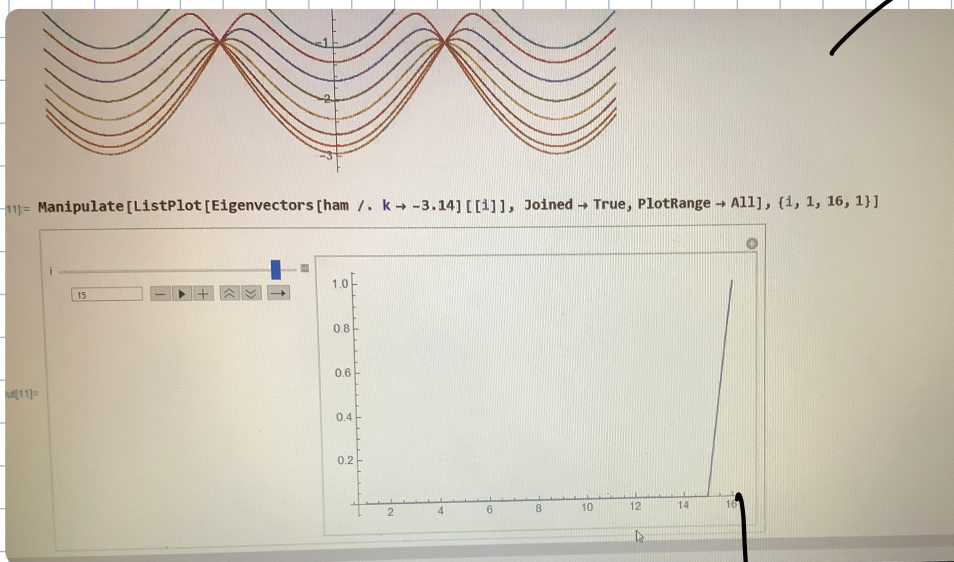
now look at eigenvectors:-

$\begin{pmatrix} | \\ | \\ | \\ | \\ | \end{pmatrix}$ → amplitude
~ weight
on a
particular
site.

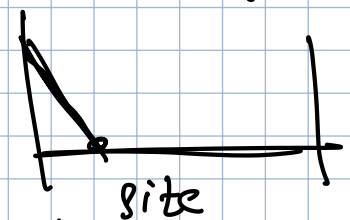


Behold the edge state:-

$$q+k = \underline{\underline{-3.14}}$$



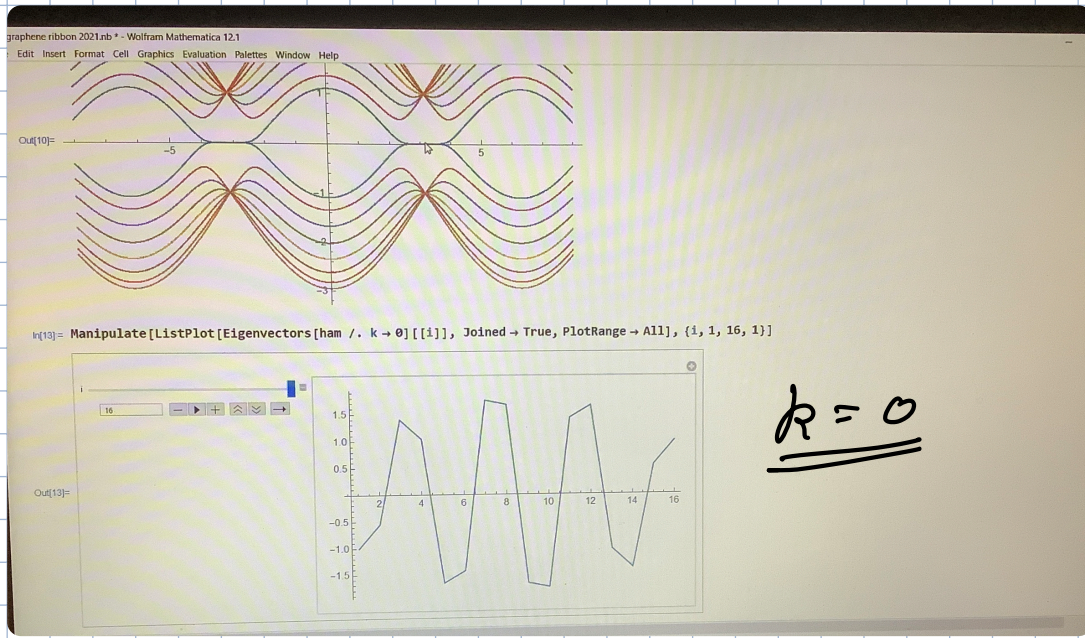
Similarly



$v_g = 0$, so they're stuck.

- eigenvectors reveal such features $\rightarrow$ reveal the effect of boundary conditions

At $k=0$, it's different:-



H.W:- Do this for Armchair GNR